

Please attempt the following questions in preparation for the online session on 2nd November 2017.

Q1

Three vectors can be expressed as follows

$$\overrightarrow{BC} = -2i - 6j + 3k$$

$$\overrightarrow{CD} = 3i + 9j - 7k$$

$$\overrightarrow{AD} = 2i + 3j + k$$

(a) Find \overrightarrow{BD} .

(b) Hence, or otherwise find \overrightarrow{BA} .

Q2

A and C are points (1, 3, -2) and (4, -3, 4) respectively.

The point B divides AC in the ratio 1:2.

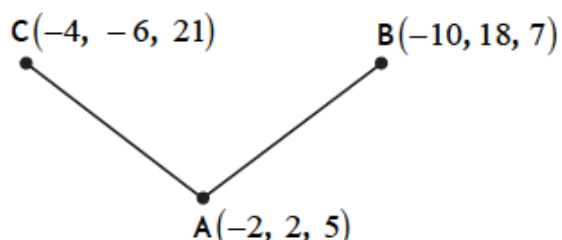
(a) Find the coordinates of B.

$k\overrightarrow{AC}$ is a vector of magnitude 1, where $k > 0$.

(b) Determine the value of k .

Q3

The points A, B and C are shown in the diagram opposite.



Find the size of $\angle BAC$?

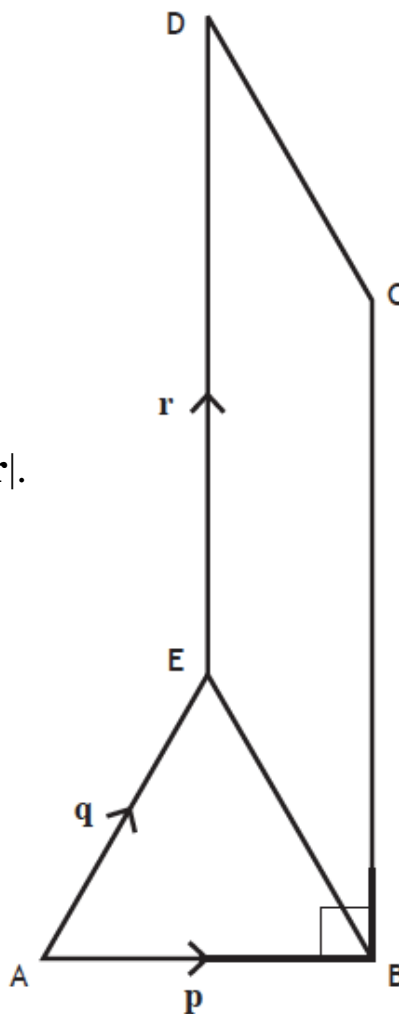
Q4 Vectors \mathbf{p} , \mathbf{q} and \mathbf{r} are represented on the diagram opposite.

- BCDE is a parallelogram
- ABE is an equilateral triangle
- $|\mathbf{p}| = 3$
- $\angle ABC = 90^\circ$

(a) Evaluate $\mathbf{p} \cdot (\mathbf{q} + \mathbf{r})$.

(b) Express \mathbf{EC} in terms of \mathbf{p} , \mathbf{q} and \mathbf{r} .

(a) Given that $\mathbf{AE} \cdot \mathbf{EC} = 9\sqrt{3} - \frac{9}{2}$, find $|\mathbf{r}|$.



Q5 Vectors $\mathbf{u} = 9\mathbf{i} + 3\mathbf{j} - \mathbf{k}$ and $\mathbf{v} = -2\mathbf{i} + a\mathbf{j} - 6\mathbf{k}$ are perpendicular. What is the value of a ?