

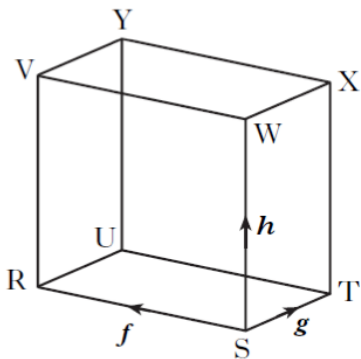
Please attempt the following questions in preparation for the online session on 9th March.

Q1

The diagram RSTUVWXY represents a cuboid.

\overrightarrow{SR} represents vector f , \overrightarrow{ST} represents vector g and \overrightarrow{SW} represents vector h .

Express \overrightarrow{VT} in terms of f , g and h .



Q2

Three vectors can be expressed as follows

$$\overrightarrow{AB} = -2\mathbf{i} - 6\mathbf{j} + 3\mathbf{k}$$

$$\overrightarrow{BC} = 3\mathbf{i} + 9\mathbf{j} - 7\mathbf{k}$$

$$\overrightarrow{EC} = 2\mathbf{i} + 3\mathbf{j} + \mathbf{k}$$

(a) Find \overrightarrow{AC} .

(b) Hence, or otherwise, find \overrightarrow{AE} .

Q3

The vector \mathbf{u} has components $\begin{pmatrix} -3 \\ 0 \\ 4 \end{pmatrix}$

Find a unit vector parallel to \mathbf{u} .

Q4

Given that $S(-4,5,1)$, $T(-16,-4,16)$ and $U(-24,-10,26)$ are collinear, calculate the ratio in which T divides SU .

Q5

Relative to a suitable coordinate system A and B are the points $(-2,1,-1)$ and $(1,3,2)$ respectively. A , B and C are collinear and C is positioned such that $BC = 2AB$.

Find the coordinates of C .

Q6

P and R are the points $(1,3,-2)$ and $(4,-3,4)$ respectively. The point Q divides PR in the ratio $1:2$.

(a) Find the coordinates of Q .

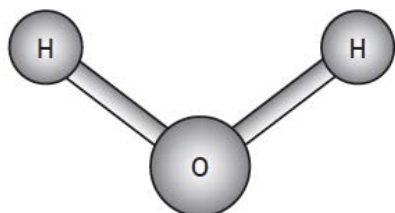
(b) $k\overrightarrow{PR}$ is a vector of magnitude 1 where $k > 0$. Determine the value of k .

Q7

Given that $QP = \begin{pmatrix} -1 \\ 3 \\ -2 \end{pmatrix}$ and $QR = \begin{pmatrix} -5 \\ 1 \\ 1 \end{pmatrix}$, find the size of angle PQR .

Q8

The diagram shows a model of a water molecule. Relative to suitable coordinate axes, the oxygen molecule is the point $Q(-2,2,5)$.



The hydrogen atoms are positioned at the points $P(-4,-6,21)$ and $R(-10,18,7)$ as in the diagram below.

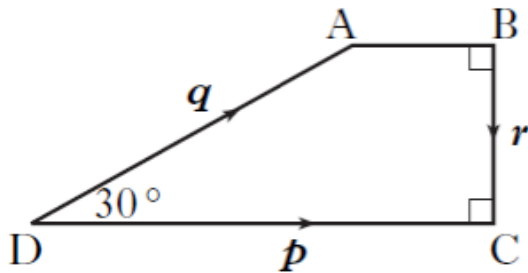


(a) Express \overrightarrow{QP} and \overrightarrow{QR} in component form.

(b) Hence, find the size of angle BAC.

Q9

The vectors \mathbf{p} , \mathbf{q} and \mathbf{r} are represented on the diagram shown, where angle $ADC = 30^\circ$.



It is also given that $|\mathbf{p}| = 4$ & $|\mathbf{q}| = 3$.

(a) Evaluate $\mathbf{p} \cdot (\mathbf{q} + \mathbf{r})$

(b) Evaluate $\mathbf{r} \cdot (\mathbf{p} - \mathbf{q})$